

CEDC403: Signals and Systems Exercises 5 & 6: Fourier Analysis for Continuous Time Signals and Systems



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Fourier Analysis for Continuous Time Signals and Systems

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1. Determine the TFS coefficients for the periodic signal shown. One period of the signal is $\tilde{x}(t) = e^{-2t}$ for 0 < t < 1 s.

The fundamental period is $T_0 = 1$ second which corresponds to a fundamental frequency of $f_0 = 1$ Hz or $\omega_0 = 2\pi$ rad/s.





2. Consider the periodic signal $\tilde{x}(t)$ of exercise 1

- a. Determine the EFS coefficients from the TFS coefficients obtained in exercise 1.
- b. Determine the EFS coefficients by direct application of the analysis equation.
- c. Sketch the line spectrum (magnitude and phase).



3. Determine the EFS coefficients of the half-wave rectified signal shown:



4. Determine the EFS coefficients of the full-wave rectified signal shown:



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5. The transform pair



Using this pair along with the duality property, find the Fourier transform of the signal





6. Using the differentiation-in-time property of the Fourier transform, determine the transform of the signal shown.





7. Determine the Fourier transform of the signal

$$x(t) = \sin(\pi t) \Pi\left(t - \frac{1}{2}\right) = \begin{cases} \sin(\pi t), & 0 < t < 1\\ 0, & \text{otherwise} \end{cases}$$

a. Using the modulation property of the Fourier transformb. Using the multiplication property of the Fourier transform



8. Consider the pulse train with duty cycle d shown. Its EFS $c_k = d \operatorname{sinc} (kd)$.

a. Working in the time domain, compute the power of the pulse train as a function of the duty cycle *d*.



- b. Sketch the power spectral density based on the EFS coefficients.
- c. Let d = 0.5. Suppose this signal is processed through a lowpass system that only retains the first m harmonics and eliminates the others. How many harmonics should be retained if we want to preserve at least 90 percent of the signal power?



- d. How many harmonics should be retained to preserve at least 95 percent of the signal power?
- e. How many harmonics should be retained to preserve at least 99 percent of the signal power?
- 9. Repeat parts (c)-(e) of Problem 8 using d = 0.2. Does it take fewer or more harmonics to preserve the same percentage of power when the duty cycle is reduced?



10. Determine and sketch the power spectral density of the following signals:

a. $x(t) = 3\cos(20\pi t)$

b. $x(t) = 2\cos(20\pi t) + 3\cos(30\pi t)$

c. $x(t) = 5\cos(200\pi t) + 5\cos(200\pi t)\cos(30\pi t)$