

ذكاء صنعي 2

محاضرة 7

# Convolutional Neural Networks

د. فادي متوج

# Computer Vision Problems



## Image Classification



→ Cat? (0/1)

## Object detection



## Neural Style Transfer



# Deep Learning on large images



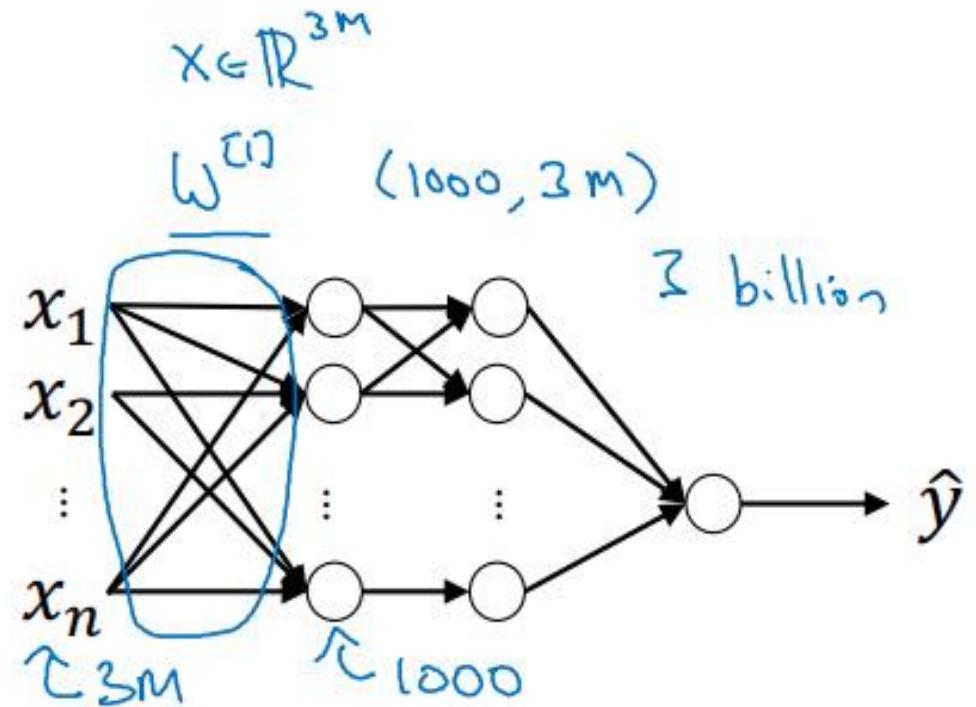
$64 \times 64 \times 3$

→ Cat? (0/1)

12288



$1000 \times 1000 \times 3$   
 $= 3 \text{ million}$





# Convolutional Neural Networks

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## Edge detection example

# Edge detection example



vertical edges

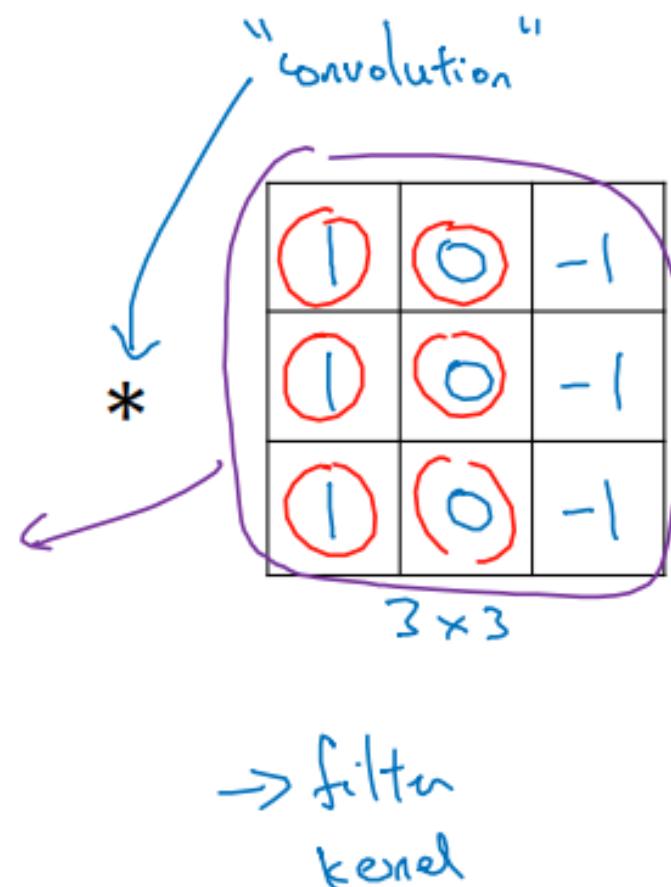


horizontal edges

$$\rightarrow 3 \times 1 + 1 \times 1 + 2 \times 1 + 0 \times 0 + 5 \times 0 + 7 \times 0 + 1 \times 1 + 8 \times -1 + 2 \times -1 = -5$$

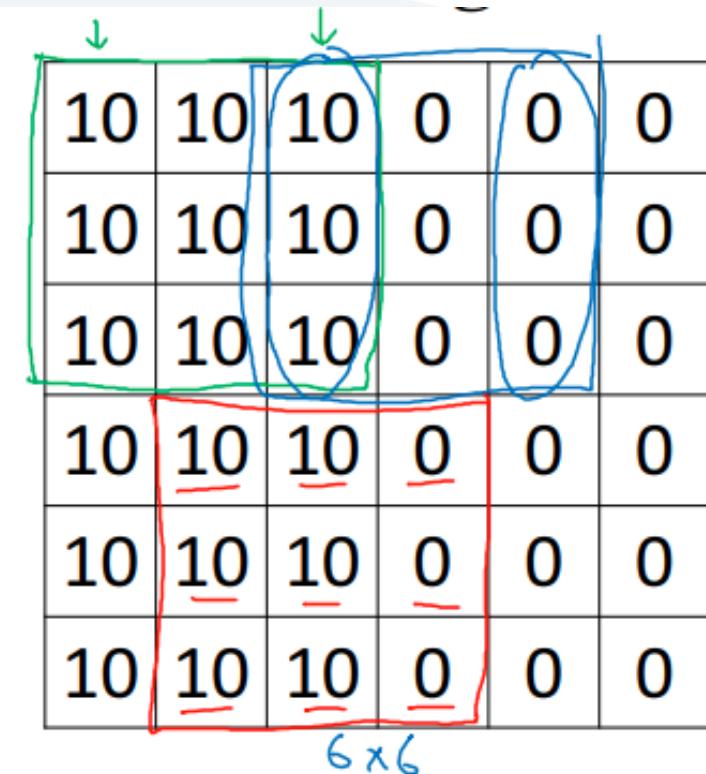
3	0	1	2	7	4
1	5	8	9	3	1
2	7	2	5	1	3
0	1	3	1	7	8
4	2	1	6	2	8
2	4	5	2	3	9

$6 \times 6$



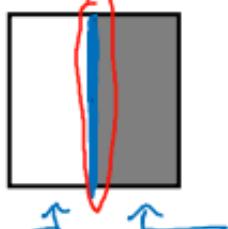
$$\begin{array}{cccc}
 -5 & -4 & 0 & 8 \\
 -10 & -2 & 2 & 3 \\
 0 & -2 & -4 & -7 \\
 -3 & -2 & -3 & \textcircled{-16} \\
 \end{array} = 
 \begin{array}{cccc}
 & & & \\
 & & & \\
 & & & \\
 & & & \\
 \end{array} \quad 4 \times 4$$

# Vertical edge detection

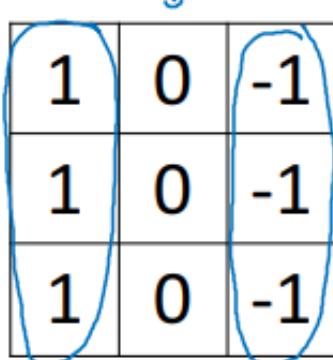


A 6x6 input matrix representing a grayscale image. The first three columns have a value of 10, while the next three columns have a value of 0. A green bracket on the left indicates the vertical edge, and a red bracket at the bottom indicates the row being processed.

10	10	10	0	0	0
10	10	10	0	0	0
10	10	10	0	0	0
10	10	10	0	0	0
10	10	10	0	0	0
10	10	10	0	0	0



\*



A 3x3 kernel for vertical edge detection. It has a value of 1 in the top row and -1 in the bottom row, with zeros in the middle row. A blue bracket encloses the entire kernel.

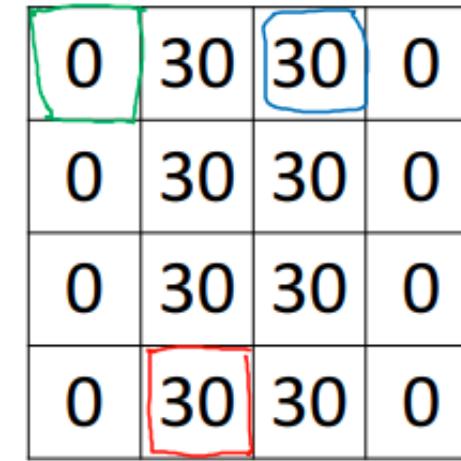
$$\begin{bmatrix} 1 & 0 & -1 \\ 1 & 0 & -1 \\ 1 & 0 & -1 \end{bmatrix}$$

$3 \times 3$

\*



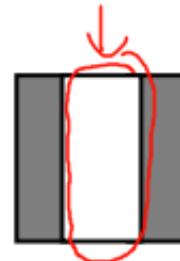
=



The result of the convolution. The first three columns are zero, and the fourth column has values 0, 30, 30, and 30. A red bracket encloses the fourth column.

$$\begin{bmatrix} 0 & 30 & 30 & 0 \\ 0 & 30 & 30 & 0 \\ 0 & 30 & 30 & 0 \\ 0 & 30 & 30 & 0 \end{bmatrix}$$

$4 \times 4$





# Convolutional Neural Networks

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More edge  
detection

## Vertical edge detection examples

10	10	10	0	0	0
10	10	10	0	0	0
10	10	10	0	0	0
10	10	10	0	0	0
10	10	10	0	0	0
10	10	10	0	0	0



0	0	0	10	10	10
0	0	0	10	10	10
0	0	0	10	10	10
0	0	0	10	10	10
0	0	0	10	10	10
0	0	0	10	10	10



\*

1	0	-1
1	0	-1
1	0	-1



=

0	30	30	0
0	30	30	0
0	30	30	0
0	30	30	0



\*

1	0	-1
1	0	-1
1	0	-1



=

0	-30	-30	0
0	-30	-30	0
0	-30	-30	0
0	-30	-30	0



# Vertical and Horizontal Edge Detection



→

1	0	-1
1	0	-1
1	0	-1

Vertical

→

1	1	1
0	0	0
-1	-1	-1

Horizontal

10	10	10	0	0	0
10	10	10	0	0	0
10	10	10	0	0	0
0	0	0	10	10	10
0	0	0	10	10	10
0	0	0	10	10	10

$6 \times 6$

\*

1	1	1
0	0	0
-1	-1	-1



=

0	0	0	0
30	10	-10	-30
30	10	-10	-30
0	0	0	0

# Learning to detect edges



1	0	-1
1	0	-1
1	0	-1

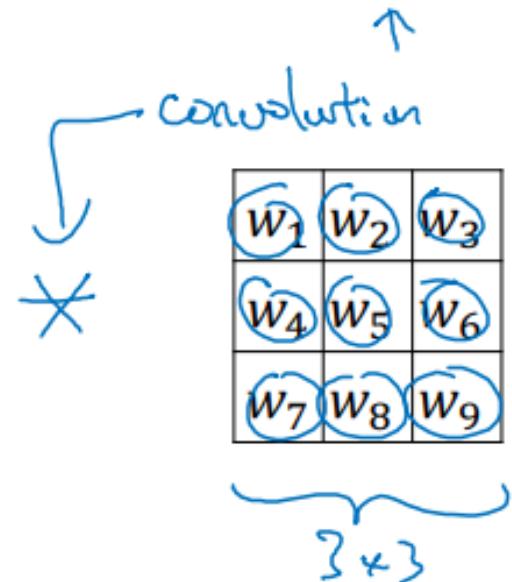


3	0	1	2	7	4
1	5	8	9	3	1
2	7	2	5	1	3
0	1	3	1	7	8
4	2	1	6	2	8
2	4	5	2	3	9

→

1	0	-1
2	0	-2
1	0	-1

Sobel filter



3	0	-3
10	0	-10
3	0	-3

Scharr filter

=


$45^\circ$   
 $70^\circ$   
 $73^\circ$

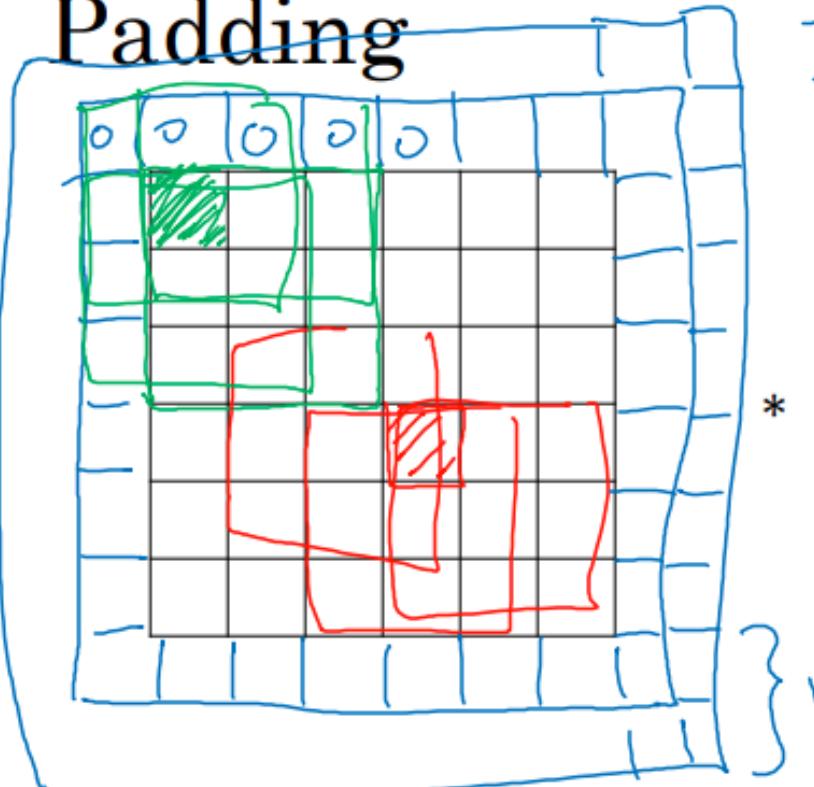


# Convolutional Neural Networks

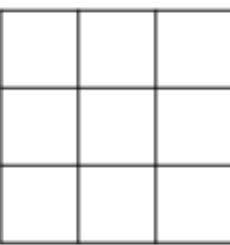
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## Padding

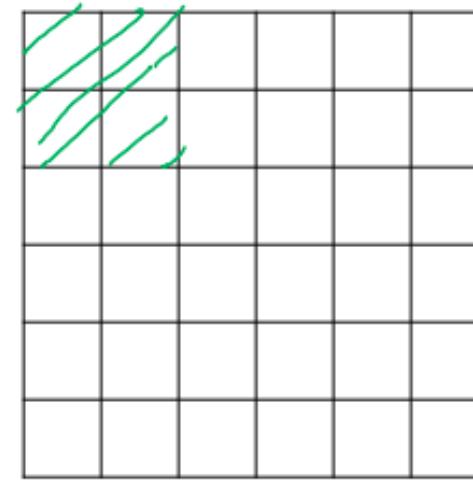
# Padding



- shrunk output
- throw away info from edge



=



$6 \times 6$

$4 \times 4$

$$\frac{6 \times L}{n \times n} \rightarrow 8 \times 8$$

$$n-f+1 \times n-f+1$$
$$6-3+1=4$$

$$P = \text{padding} = 1$$

$$n+2p-f+1 \times n+2p-f-1$$
$$6+2-3+1 \times \underline{\quad} = 6 \times 6$$

## Valid and Same convolutions



→  $n = \text{padding}$

“Valid”:  $n \times n \times f \times f \rightarrow \frac{n-f+1}{f} \times \frac{n-f+1}{f}$

$$6 \times 6 \times 3 \times 3 \rightarrow 4 \times 4$$

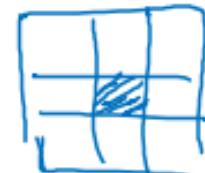
“Same”: Pad so that output size is the same as the input size.

$$n + 2p - f + 1 \times n + 2p - f + 1$$

$$\cancel{n + 2p - f + 1} = n \Rightarrow p = \frac{f-1}{2}$$

$$3 \times 3 \quad p = \frac{3-1}{2} = 1 \quad \left| \begin{array}{c} 5 \times 5 \\ f=5 \end{array} \right. \quad p=2$$

$f$  is usually odd  
 $1 \times 1$   
 $3 \times 3$   
 $5 \times 5$   
 $7 \times 7$



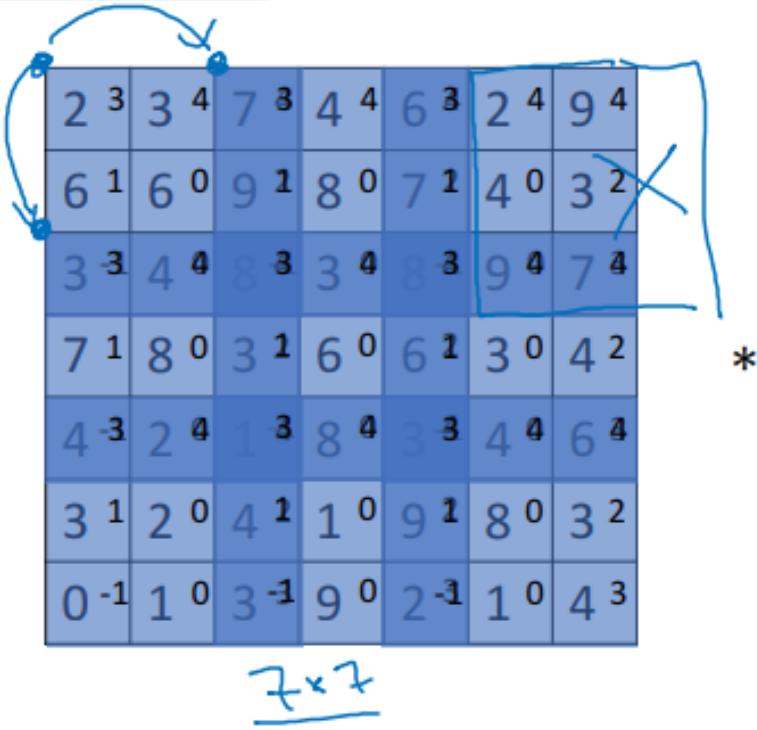


# Convolutional Neural Networks

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## Strided convolutions

# Strided convolution



$n \times n$  \*  $f \times f$   
padding p      strides s  
 $s=2$

$$\begin{array}{|c|c|c|} \hline 3 & 4 & 4 \\ \hline 1 & 0 & 2 \\ \hline -1 & 0 & 3 \\ \hline \end{array} = \begin{array}{|c|c|c|} \hline 91 & 100 & 83 \\ \hline 69 & 91 & 127 \\ \hline 44 & 72 & 74 \\ \hline \end{array}$$

$\frac{3 \times 3}{3 \times 3}$

stride = 2       $\lfloor z \rfloor = \text{floor}(z)$

$$\left\lfloor \frac{n+2p-f}{s} + 1 \right\rfloor \times \left\lfloor \frac{n+2p-f}{s} + 1 \right\rfloor$$
$$\frac{7+0-3}{2} + 1 = \frac{4}{2} + 1 = 3$$

# Summary of convolutions



$n \times n$  image

$f \times f$  filter

padding  $p$

stride  $s$

Output size:

$$\left\lfloor \frac{n+2p-f}{s} + 1 \right\rfloor \quad \times \quad \left\lfloor \frac{n+2p-f}{s} + 1 \right\rfloor$$

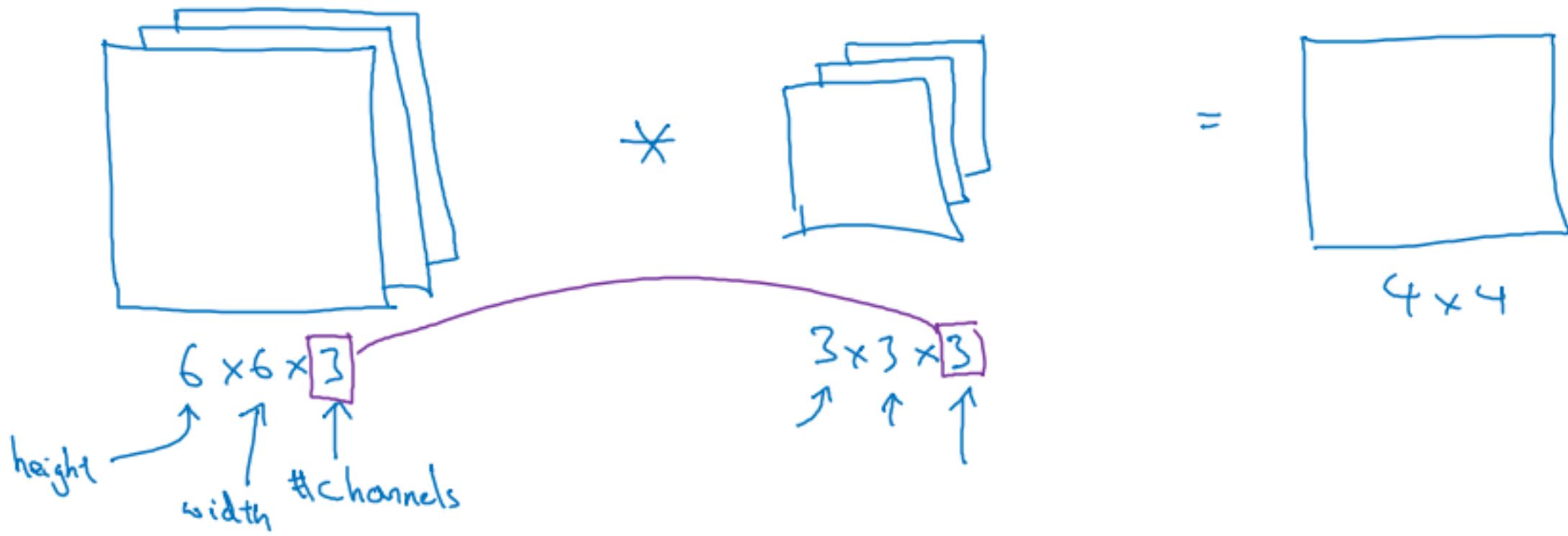


# Convolutional Neural Networks

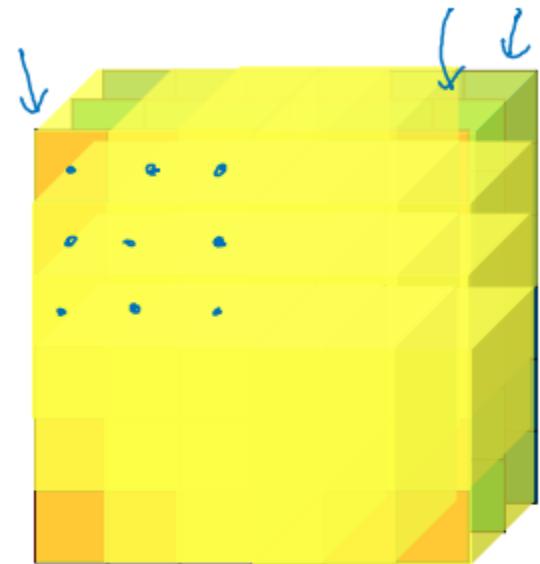
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## Convolutions over volumes

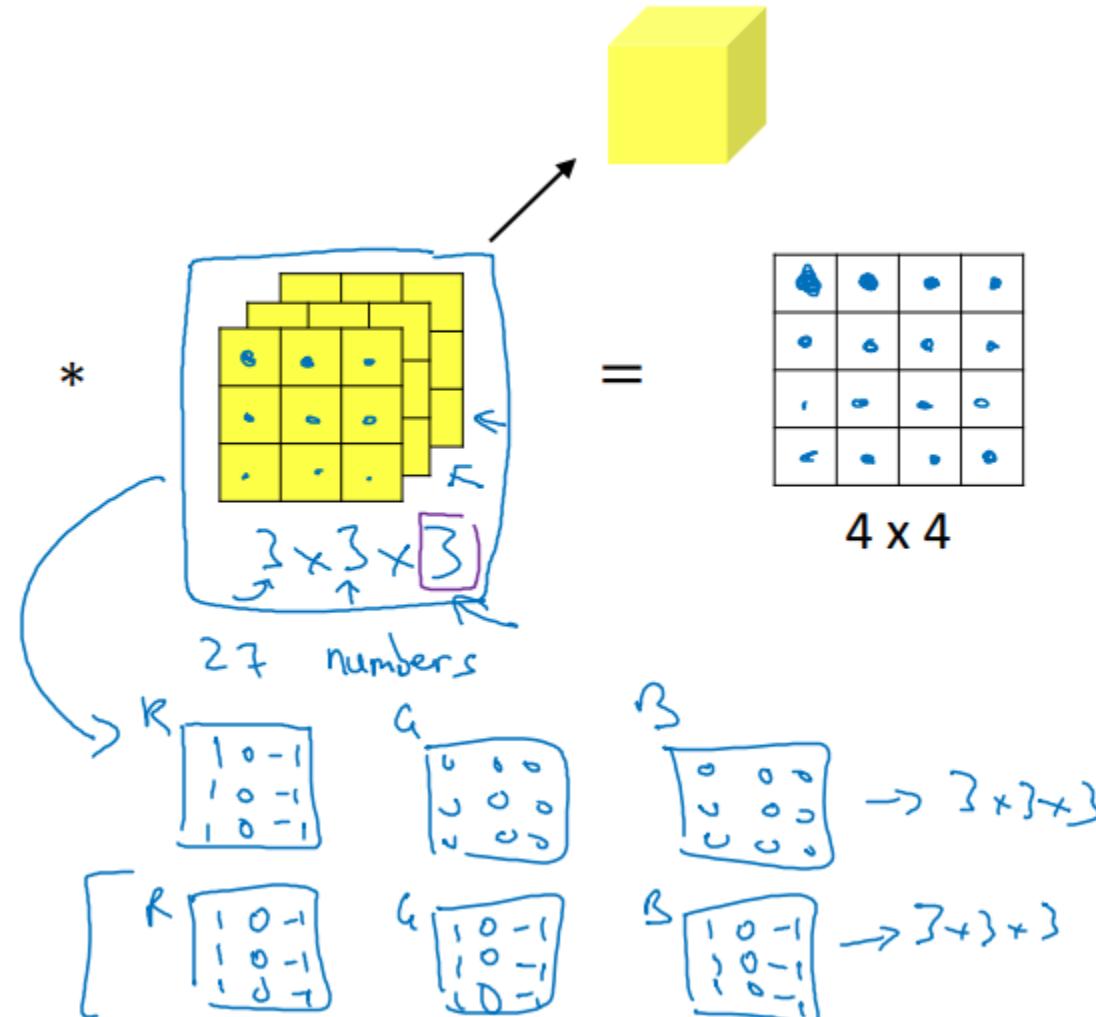
# Convolutions on RGB images



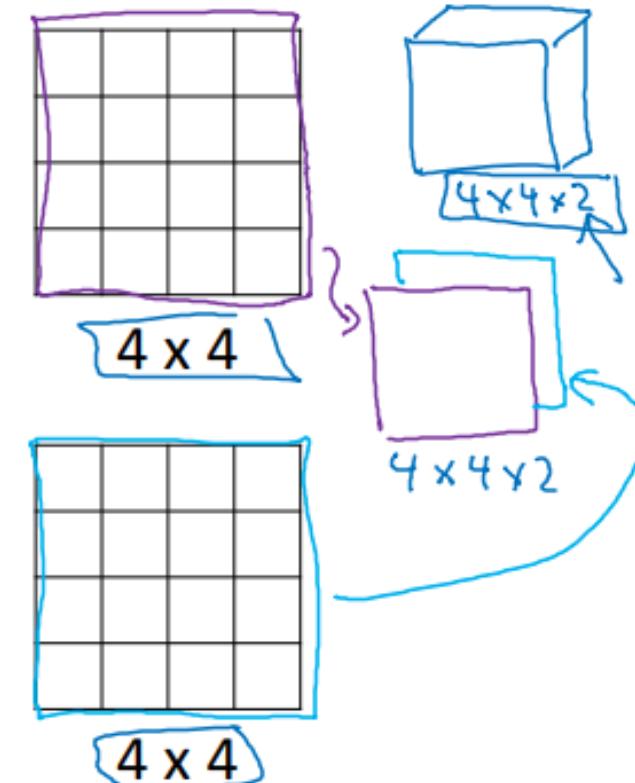
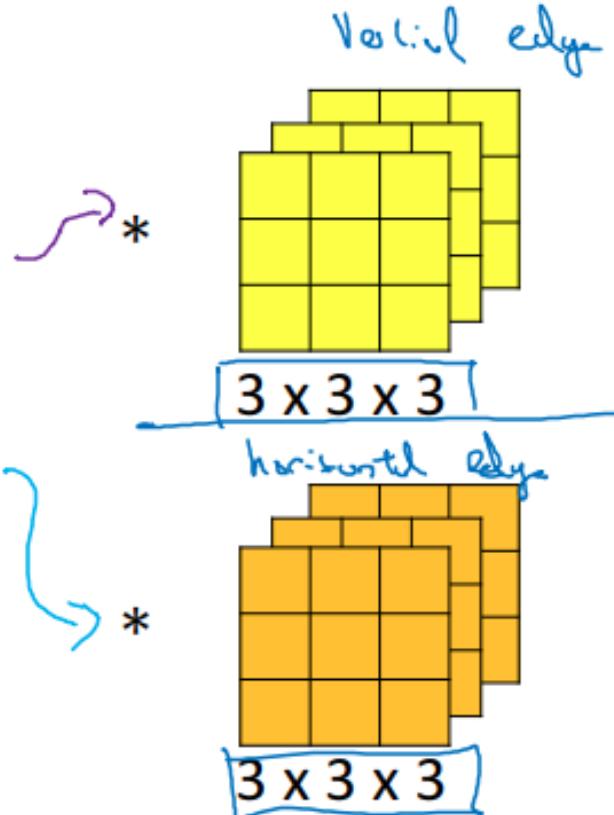
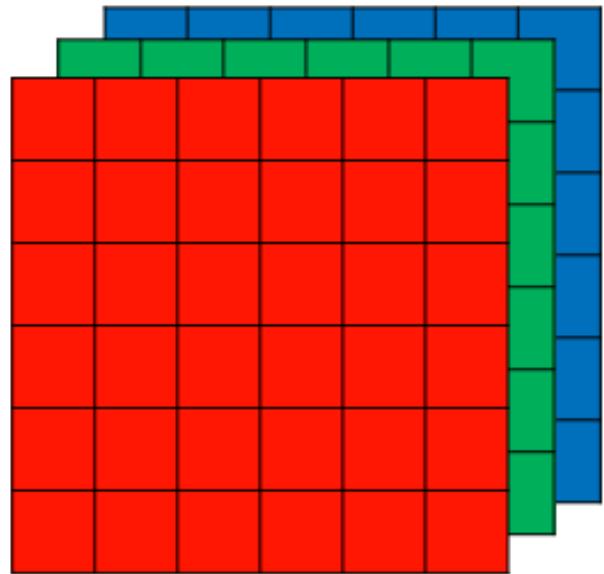
# Convolutions on RGB image



$$\begin{array}{c} \boxed{\text{cube}} * \boxed{\text{cube}} = \boxed{\text{square}} \\ \uparrow \quad \uparrow \quad \uparrow \\ \text{cube} \end{array}$$



# Multiple filters



Summary:  $n \times n \times n_c$   $\times f \times f \times n_c$   $\rightarrow \frac{n-f+1}{4} \times \frac{n-f+1}{4} \times \frac{n_c}{2} \# \text{filters}$

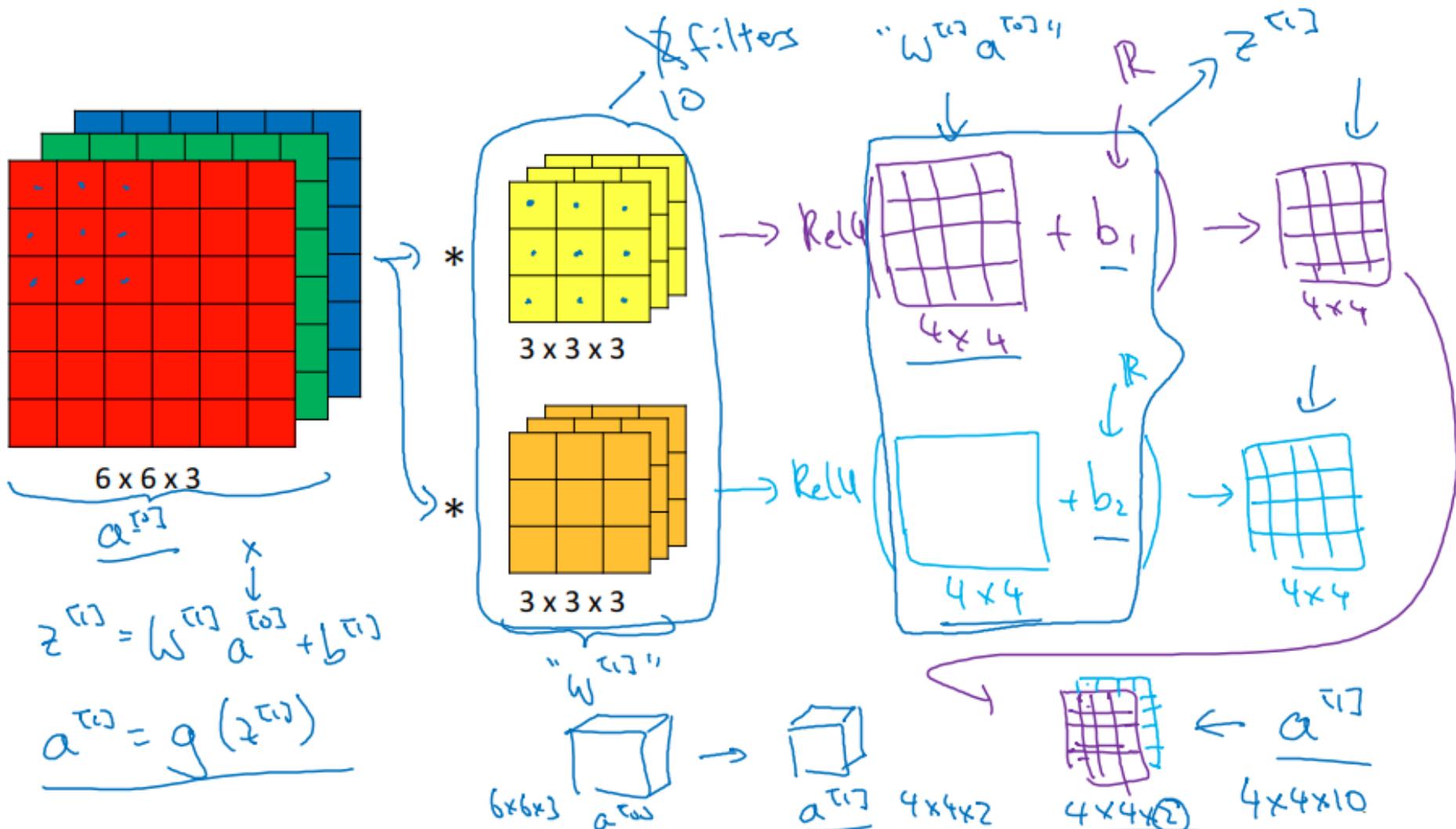


# Convolutional Neural Networks

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**One layer of a  
convolutional  
network**

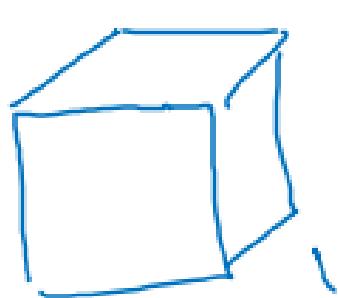
# Example of a layer



## Number of parameters in one layer



If you have 10 filters that are  $3 \times 3 \times 3$  in one layer of a neural network, how many parameters does that layer have?

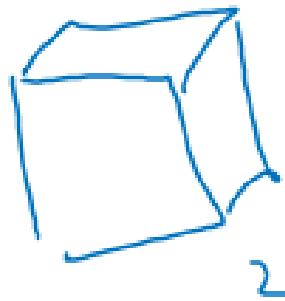


$$3 \times 3 \times 3$$

27 parameters.

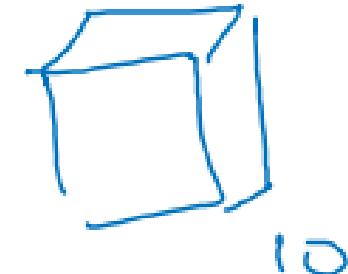
+ bias

→ 28 parameters.



$$2$$

...  
...



$$10$$

280 parameters.

# Summary of notation

If layer  $\underline{l}$  is a convolution layer:

$f^{[l]}$  = filter size

$p^{[l]}$  = padding

$s^{[l]}$  = stride

$n_c^{[l]}$  = number of filters

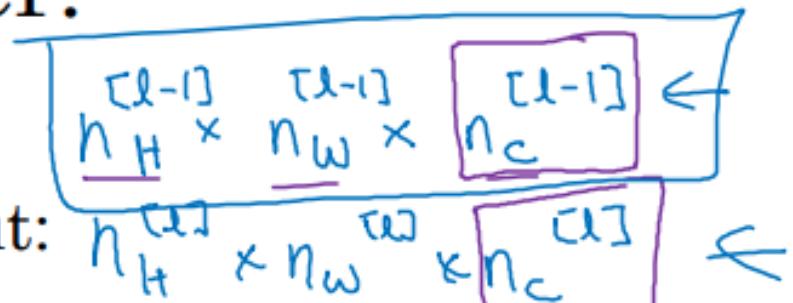
→ Each filter is:  $f^{[l]} \times f^{[l]} \times n_c^{[l]}$

Activations:  $A^{[l]} \rightarrow n_H^{[l]} \times n_w^{[l]} \times n_c^{[l]}$ .

Weights:  $f^{[l]} \times f^{[l]} \times n_c^{[l-1]} \times n_c^{[l]}$

bias:  $n_c^{[l]} = (1, 1, 1, n_c^{[l]})$  #f: filters in layer l.

Input:



Output:

$$\frac{n_{Hw}^{[l-1]} + 2p^{[l]} - f^{[l]}}{s^{[l]}} + 1$$

$$A^{[l]} \rightarrow m \times \underbrace{n_H^{[l]} \times n_w^{[l]}}_{n_{Hw}^{[l]}} \times n_c^{[l]}$$

$$\underbrace{n_c^{[l-1]} \times n_c^{[l]}}$$

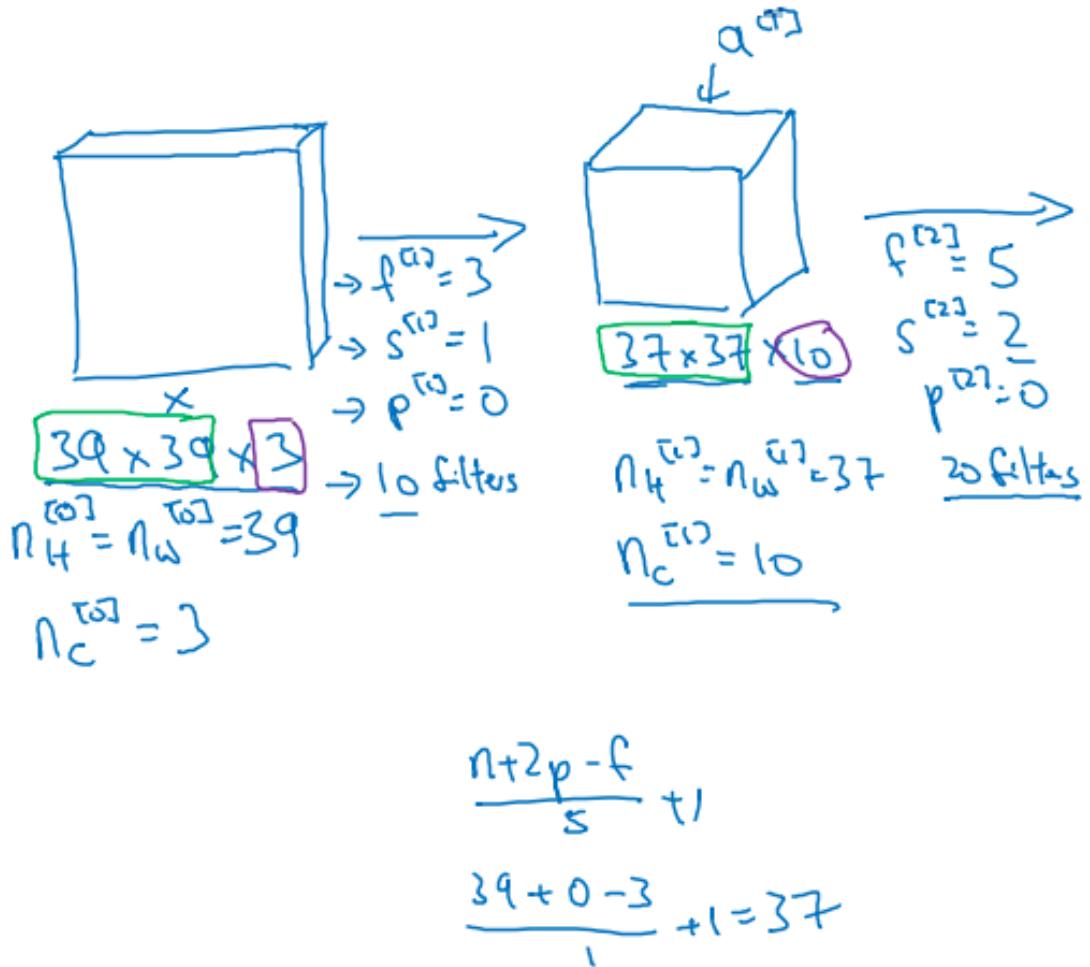


# Convolutional Neural Networks

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**A simple convolution  
network example**

# Example ConvNet



## Types of layer in a convolutional network:

- Convolution
- Pooling
- Fully connected



# Convolutional Neural Networks

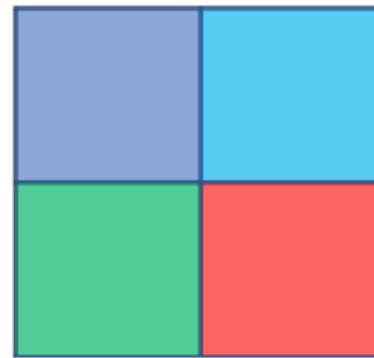
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## Pooling layers

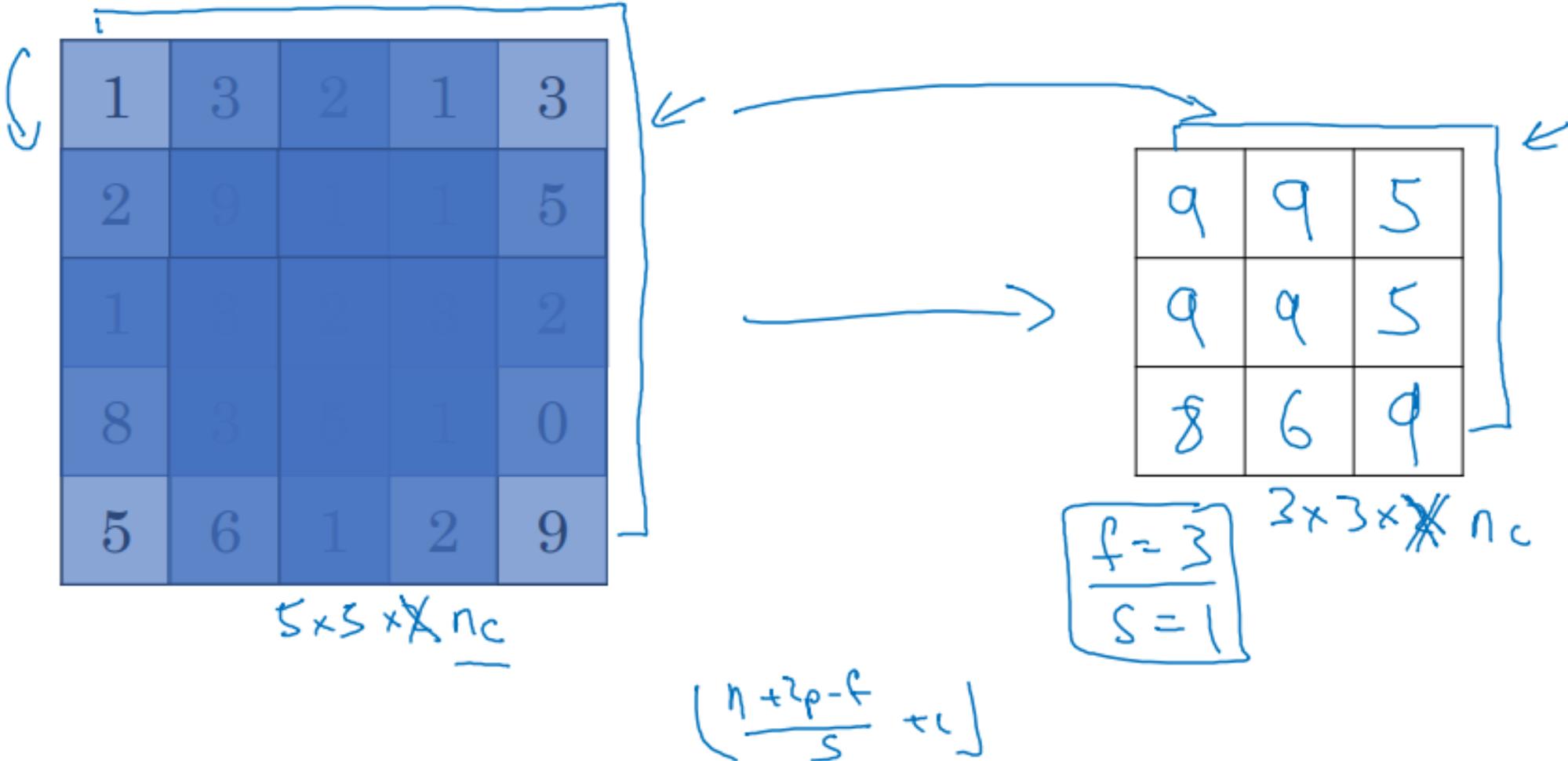
# Pooling layer: Max pooling



1	3	2	1
2	9	1	1
1	3	2	3
5	6	1	2



# Pooling layer: Max pooling



# Pooling layer: Average pooling



1	3	2	1
2	9	1	1
1	4	2	3
5	6	1	2



3.75	1.25
4	2

$$f = 2$$

$$s = 2$$

$$\underbrace{7 \times 7 \times 1000} \rightarrow 1 \times 1 \times 1000$$

# Summary of pooling



Hyperparameters:

$f$  : filter size

$s$  : stride

Max or average pooling

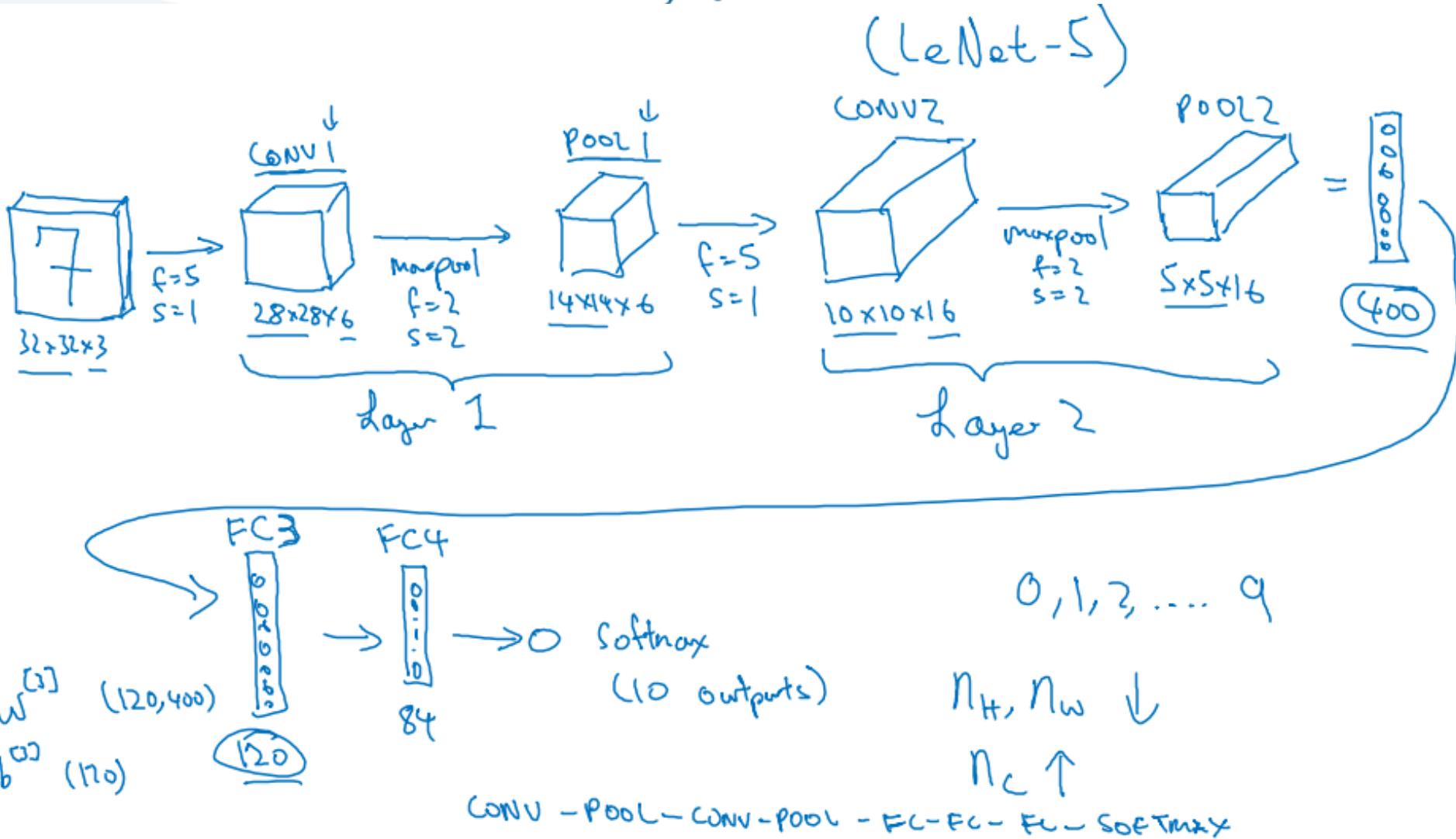


# Convolutional Neural Networks

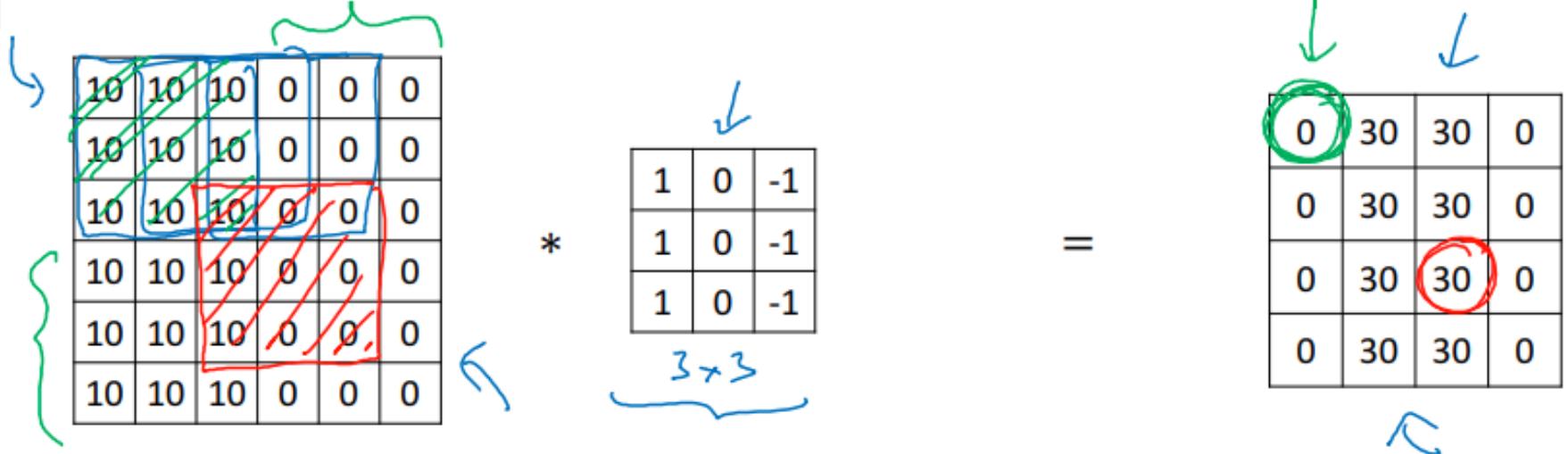
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## Convolutional neural network example

# Neural network example



# Why convolutions



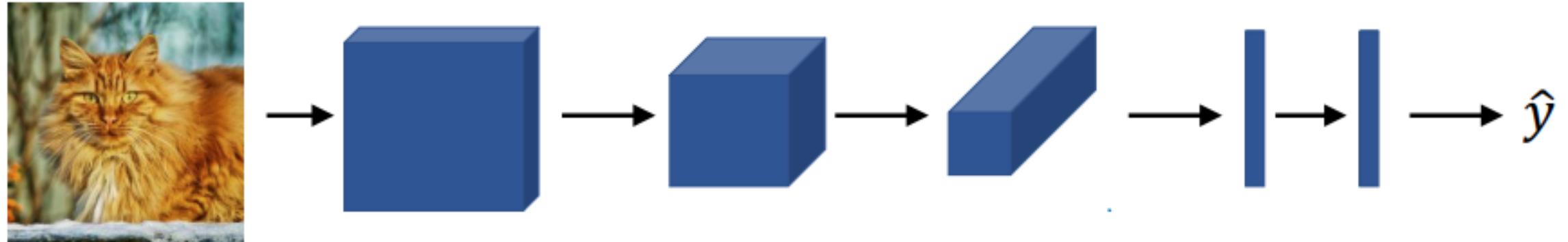
**Parameter sharing:** A feature detector (such as a vertical edge detector) that's useful in one part of the image is probably useful in another part of the image.

→ **Sparsity of connections:** In each layer, each output value depends only on a small number of inputs.

# Putting it together



Training set  $(x^{(1)}, y^{(1)}) \dots (x^{(m)}, y^{(m)})$ .



$$\text{Cost } J = \frac{1}{m} \sum_{i=1}^m \mathcal{L}(\hat{y}^{(i)}, y^{(i)})$$

Use gradient descent to optimize parameters to reduce  $J$