

Problem 1. If $\vec{p} = 2\hat{i} + \hat{j} - \hat{k}$ and $\vec{q} = \hat{i} - 3\hat{j} + 2\hat{k}$.

1. Represent the two vectors in a three dimensional orthonormal coordinate system.
2. Find $\vec{p} + \vec{q}$. Then represent it on the same coordinate system.
3. Find $|\vec{p}|$, $|\vec{q}|$ and $|\vec{p} + \vec{q}|$.
4. Find $\vec{p} \cdot \vec{q}$, then find the angle between \vec{p} and \vec{q}

Problem 2. If $\vec{p} = 4\hat{i} + \hat{j} - 2\hat{k}$, $\vec{q} = 3\hat{i} - 2\hat{j} + \hat{k}$ and $\vec{r} = \hat{i} - 2\hat{j}$

1. Represent the three vectors in a three dimensional orthonormal coordinate system.
2. Find $(\vec{p} - 2\vec{q}) \times \vec{r}$.
3. Find $\vec{p} \times (2\vec{r} \times 3\vec{q})$

Problem 3. For the vectors $\vec{a} = \hat{i} + 4\hat{j} - 2\hat{k}$ and $\vec{b} = 2\hat{i} - \hat{j} + 3\hat{k}$.

1. Represent the two vectors in a three dimensional orthonormal coordinate system.
2. Find $\vec{a} \times \vec{b}$. Then represent it on the same coordinate system.

Problem 4. Represent the two vectors $\vec{a} = 2\hat{i} - \hat{j} + 3\hat{k}$ and $\vec{b} = -\hat{i} + \hat{j} - 3\hat{k}$ in a three-dimensional orthonormal coordinate system.

Find the angle between the two vectors. Then

Find $\vec{a} \times \vec{b}$. Then represent it on the same coordinate system.

Problem 5. For the vector $\vec{r} = 2\hat{i} + 5\hat{j} + 13\hat{k}$

1) Sketch the vector in a three-dimensional orthonormal coordinate system.

2) Find its length. Then

3) Find the direction cosines and the angles the vector makes with coordinate axes.

Problem 6. sketch the three vectors: $\vec{a} = 2\hat{i} + \hat{j} - \hat{k}$, $\vec{b} = \hat{i} - 3\hat{j} + 2\hat{k}$ and $\vec{c} = 2\hat{i} - \hat{j} + 3\hat{k}$, then find the oriented volume (الحجم الموجه) of the parallelepiped (متوازي سطوح) defined by these vectors.

Problem 7. If $\vec{p} = 2\hat{i} + \hat{j} + \hat{k}$ and $\vec{q} = \hat{i} + 2\hat{j} + 2\hat{k}$.

1. Represent the two vectors in a three dimensional orthonormal coordinate system.
2. Find $\vec{p} + \vec{q}$. Then represent it on the same coordinate system.
3. Find $|\vec{p}|$, $|\vec{q}|$ and $|\vec{p} + \vec{q}|$.
4. Find $\vec{p} \cdot \vec{q}$, then find the angle between \vec{p} and \vec{q}

Problem 8. If $\vec{p} = 4\hat{i} + \hat{j} - \hat{k}$, $\vec{q} = 3\hat{i} - \hat{j} + \hat{k}$ and $\vec{r} = \hat{i} - \hat{j}$

1. Represent the three vectors in a three dimensional orthonormal coordinate system.
2. Find $(\vec{p} - 2\vec{q}) \times \vec{r}$.
3. Find $\vec{p} \times (2\vec{r} \times 3\vec{q})$

Problem 9. For the vectors $\vec{a} = -\hat{i} + \hat{j} - \hat{k}$ and $\vec{b} = 2\hat{i} - \hat{j} + \hat{k}$.

1. Represent the two vectors in a three dimensional orthonormal coordinate system.
2. Find $\vec{a} \times \vec{b}$. Then represent it on the same coordinate system.

All calculators have **+**, **-**, **x** and **÷** functions and these functions will, no doubt, already have been used in calculations.

Problem 1. Evaluate $364.7 \div 57.5$ correct to 3 decimal places

- (i) Type in 364.7
- (ii) Press \div .
- (iii) Type in 57.5
- (iv) Press = and the fraction $\frac{3647}{575}$ appears.
- (v) Press the $S \Leftrightarrow D$ function and the decimal answer 6.34260869... appears.

Alternatively, after step (iii) press Shift and = and the decimal will appear.

Hence, $364.7 \div 57.5 = 6.343$, correct to 3 decimal places.

Problem 2. Evaluate $\frac{12.47 \times 31.59}{70.45 \times 0.052}$ correct to 4 significant figures

- (i) Type in 12.47
- (ii) Press \times .
- (iii) Type in 31.59
- (iv) Press \div .
- (v) The denominator must have brackets; i.e. press (.
- (vi) Type in 70.45×0.052 and complete the bracket; i.e. press)
- (vii) Press = and the answer 107.530518... appears.

Hence, $\frac{12.47 \times 31.59}{70.45 \times 0.052} = 107.5$, correct to 4 significant figures.

Now try the following Practice Exercise

Practice Exercise 12 Addition, subtraction, multiplication and division using a calculator (answers on page 1149)

1. Evaluate $378.37 - 298.651 + 45.64 - 94.562$
2. Evaluate 25.63×465.34 correct to 5 significant figures.
3. Evaluate $562.6 \div 41.3$ correct to 2 decimal places.
4. Evaluate $\frac{17.35 \times 34.27}{41.53 \div 3.76}$ correct to 3 decimal places.
5. Evaluate $27.48 + 13.72 \times 4.15$ correct to 4 significant figures.
6. Evaluate $\frac{(4.527 + 3.63)}{(452.51 \div 34.75)} + 0.468$ correct to 5 significant figures.

7. Evaluate $52.34 - \frac{(912.5 \div 41.46)}{(24.6 - 13.652)}$ correct to 3 decimal places.
8. Evaluate $\frac{52.14 \times 0.347 \times 11.23}{19.73 \div 3.54}$ correct to 4 significant figures.
9. Evaluate $\frac{451.2}{24.57} - \frac{363.8}{46.79}$ correct to 4 significant figures.
10. Evaluate $\frac{45.6 - 7.35 \times 3.61}{4.672 - 3.125}$ correct to 3 decimal places.

4.3 Further calculator functions

Square and cube functions

Locate the x^2 and x^3 functions on your calculator and then check the following worked examples.

Problem 3. Evaluate 2.4^2

- (i) Type in 2.4
- (ii) Press x^2 and 2.4^2 appears on the screen.
- (iii) Press = and the answer $\frac{144}{25}$ appears.
- (iv) Press the $S \leftrightarrow D$ function and the fraction changes to a decimal: 5.76

Alternatively, after step (ii) press Shift and = .
Thus, $2.4^2 = 5.76$

Problem 4. Evaluate 0.17^2 in engineering form

- (i) Type in 0.17
- (ii) Press x^2 and 0.17^2 appears on the screen.
- (iii) Press Shift and = and the answer 0.0289 appears.
- (iv) Press the ENG function and the answer changes to 28.9×10^{-3} , which is **engineering form**.

Hence, $0.17^2 = 28.9 \times 10^{-3}$ in engineering form. The ENG function is extremely important in engineering calculations.

Problem 5. Change 348620 into engineering form

- (i) Type in 348620
- (ii) Press = then ENG.

Hence, $348620 = 348.62 \times 10^3$ in engineering form.

Problem 6. Change 0.0000538 into engineering form

- (i) Type in 0.0000538
- (ii) Press = then ENG.

Hence, $0.0000538 = 53.8 \times 10^{-6}$ in engineering form.

Problem 7. Evaluate 1.4^3

- (i) Type in 1.4
- (ii) Press x^3 and 1.4^3 appears on the screen.
- (iii) Press = and the answer $\frac{343}{125}$ appears.
- (iv) Press the $S \Leftrightarrow D$ function and the fraction changes to a decimal: 2.744

Thus, $1.4^3 = 2.744$

Now try the following Practice Exercise

Practice Exercise 13 Square and cube functions (answers on page 1149)

1. Evaluate 3.5^2
2. Evaluate 0.19^2
3. Evaluate 6.85^2 correct to 3 decimal places.
4. Evaluate $(0.036)^2$ in engineering form.
5. Evaluate 1.563^2 correct to 5 significant figures.
6. Evaluate 1.3^3
7. Evaluate 3.14^3 correct to 4 significant figures.
8. Evaluate $(0.38)^3$ correct to 4 decimal places.
9. Evaluate $(6.03)^3$ correct to 2 decimal places.
10. Evaluate $(0.018)^3$ in engineering form.

Square and cube functions

Locate the x^2 and x^3 functions on your calculator and then check the following worked examples.

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- (iv) Press the $S \Leftrightarrow D$ function and the fraction changes to a decimal: 2.744

Thus, $1.4^3 = 2.744$

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Reciprocal and power functions

The reciprocal of 2 is $\frac{1}{2}$, the reciprocal of 9 is $\frac{1}{9}$ and the reciprocal of x is $\frac{1}{x}$, which from indices may be written as x^{-1} . Locate the reciprocal, i.e. x^{-1} , on the calculator. Also, locate the power function, i.e. x^{\square} , on your calculator and then check the following worked examples.

Problem 8. Evaluate $\frac{1}{3.2}$

- (i) Type in 3.2
- (ii) Press x^{-1} and 3.2^{-1} appears on the screen.
- (iii) Press = and the answer $\frac{5}{16}$ appears.
- (iv) Press the $S \Leftrightarrow D$ function and the fraction changes to a decimal: 0.3125

Thus, $\frac{1}{3.2} = 0.3125$

Problem 9. Evaluate 1.5^5 correct to 4 significant figures

- (i) Type in 1.5
- (ii) Press x^{\square} and 1.5^{\square} appears on the screen.
- (iii) Press 5 and 1.5^5 appears on the screen.
- (iv) Press Shift and = and the answer 7.59375 appears.

Thus, $1.5^5 = 7.594$, correct to 4 significant figures.

Problem 10. Evaluate $2.4^6 - 1.9^4$ correct to 3 decimal places

- (i) Type in 2.4
- (ii) Press x^{\square} and 2.4^{\square} appears on the screen.
- (iii) Press 6 and 2.4^6 appears on the screen.
- (iv) The cursor now needs to be moved; this is achieved by using the cursor key (the large blue circular function in the top centre of the calculator). Press \rightarrow
- (v) Press $-$
- (vi) Type in 1.9, press x^{\square} , then press 4
- (vii) Press = and the answer 178.07087... appears.

Thus, $2.4^6 - 1.9^4 = 178.071$, correct to 3 decimal places.

Now try the following Practice Exercise

Practice Exercise 14 Reciprocal and power functions (answers on page 1149)

1. Evaluate $\frac{1}{1.75}$ correct to 3 decimal places.
2. Evaluate $\frac{1}{0.0250}$
3. Evaluate $\frac{1}{7.43}$ correct to 5 significant figures.
4. Evaluate $\frac{1}{0.00725}$ correct to 1 decimal place.
5. Evaluate $\frac{1}{0.065} - \frac{1}{2.341}$ correct to 4 significant figures.
6. Evaluate 2.1^4
7. Evaluate $(0.22)^5$ correct to 5 significant figures in engineering form.
8. Evaluate $(1.012)^7$ correct to 4 decimal places.
9. Evaluate $(0.05)^6$ in engineering form.
10. Evaluate $1.1^3 + 2.9^4 - 4.4^2$ correct to 4 significant figures.